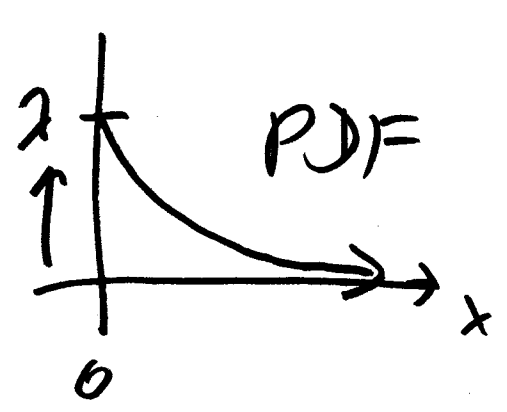


this time: transformations
 next time: expected value, variance,
 standard deviation, covariance,
 correlation

read: STAT 131
 14 May 20
 (lecture)
 DS ch. 4

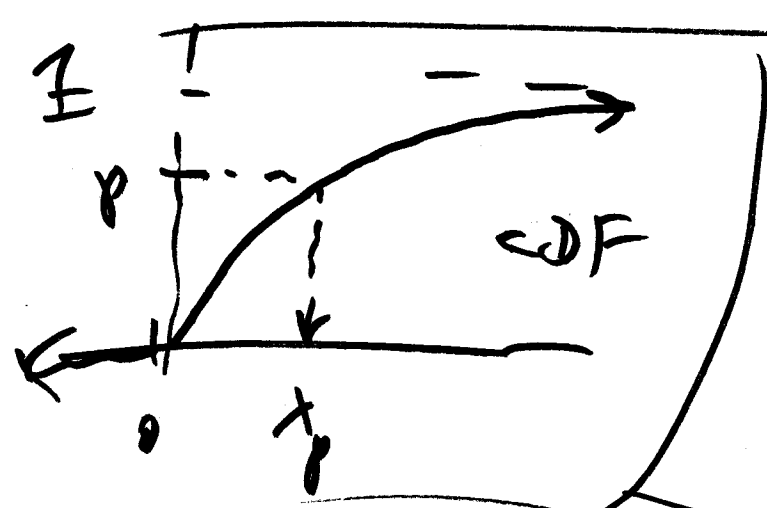
①

$(X | \lambda) \sim \text{Exponential}(\lambda)$



PDF

$$f_X(x) = \begin{cases} \lambda e^{-\lambda x} & \text{for } x \geq 0 \\ 0 & \text{else} \end{cases}$$

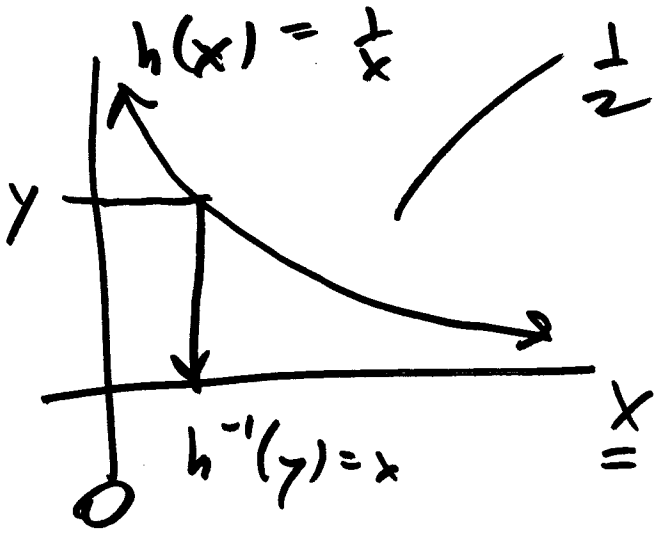


CDF

$$F_X(x) = \begin{cases} 0 & \text{for } x < 0 \\ 1 - e^{-\lambda x} & \text{for } x \geq 0 \end{cases}$$

$p = 1 - e^{-\lambda x_p}$
 $0 < p < 1$

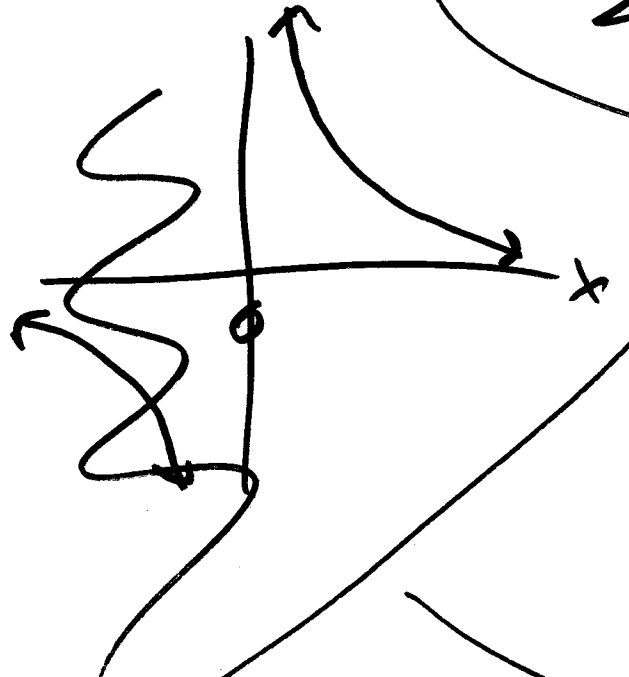
$F_X^{-1}(p) = -\frac{\log(1-p)}{\lambda}$



$\frac{1}{2}$ of a hyperbola

$h(x)$ diff. on $(0, \infty)$? **yes**

$\mathbb{R}^2 (1-1) \text{ or } \mathbb{R}$



functions
(+ transformations)
of a r.v. or
a random vector:

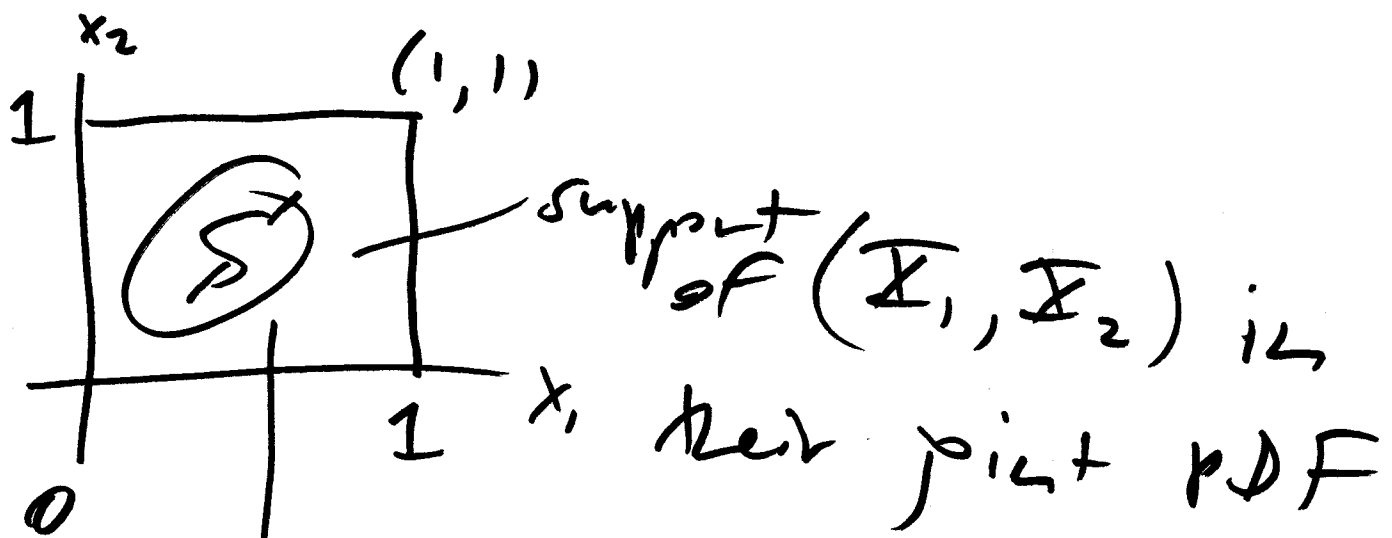
DS sec. 3.8, 3.9

$$\begin{cases} x_1 = \gamma_1 \\ x_2 = \gamma_2 \\ x_1, x_2 = \gamma_2 \end{cases}$$

$$x_1 = \gamma_1 \cdot x_2 = \gamma_1 \cdot \gamma_2$$

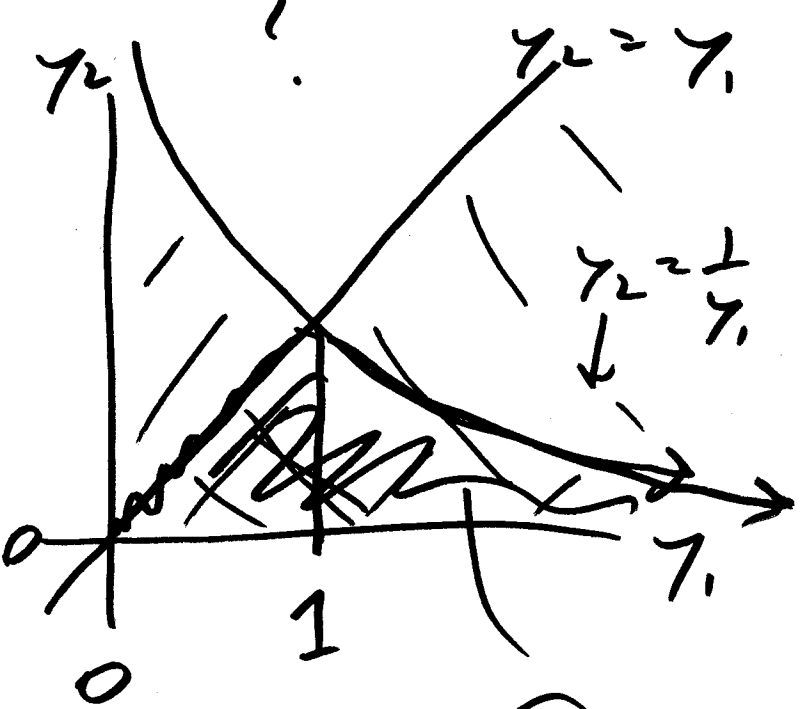
$$x_2 = \frac{\gamma_2}{x_1}$$

$$x_1 = \sqrt{\gamma_1 \cdot \gamma_2}$$



(h_1, h_2)

?



$$y_2 < \frac{1}{y_1}$$

$$y_2 < y_1$$

(T) = support of (Y_1, Y_2)