

D office  
1.5 hour  
21 Apr 20

table 3

$$P(D \text{ and } S) = \frac{139}{1314}$$

STAT 131  
21 Apr 20

①

$$P(D | \text{not } S) = \frac{230}{732}$$

association  
between  $X$   
and  $Z$

as smoking goes from (never smoked) to

(current smoker) in the 1970s, (table 3)

$$P(\text{dead} | \text{never smoked}) > P(\text{dead} | \text{current smoker})$$

$P(\text{dead}) \downarrow (!)$

assoc. betw.  $X$  and  $Z$   
smoking  $\uparrow$  age  $\uparrow$

or  $X \uparrow Z \downarrow$

assoc. betw.  $S$  and  $Z$   
as  $Z \uparrow S \uparrow$  dead  $\uparrow$  age

P(at least 1 GP winner in this draw) <sup>②</sup>

→ grand prize = ?

meta-code  
(process)

how to  
solve  
applied  
math  
problems

when solving a new problem  
 $P_{new}$ , try to find another  
problem  $P_{old}$  with

2 properties: {  
①  $P_{old}$ ,  $P_{new}$  similar  
in relevant ways  
② you know how  
to solve  $P_{old}$

T-5:

P(1 or more T-5 babies in  
5 kids, both parents  
carriers)

P(1 or more (interesting things) happening  
IID  $P(T_5) = \frac{1}{4}$ )

⊛ in  $n$  trials  $\leftarrow$  ⊛,  $P(\text{⊛}) = p$  = ?

$$T-5 \text{ } \textcircled{*} = 1 - \left(1 - \frac{1}{4}\right)^5$$

$$\textcircled{**} = 1 - (1 - p)^n$$

(interesting thing  $\textcircled{I}$ )  $\leftrightarrow$  person  $j$  wills GP  
for person  $i$

$$P(\textcircled{I}) = p = \frac{1}{292,201,338}$$

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$$n = 182,900,000$$

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$$P(8,17) = P\left(\begin{matrix} \text{all } 5 \\ w \end{matrix} \text{ and } \begin{matrix} 0 \\ R \end{matrix}\right)$$

$$= \text{w, R indep } P\left(\begin{matrix} \text{all } 5 \\ w \end{matrix}\right) \cdot P\left(\begin{matrix} 0 \\ R \end{matrix}\right)$$

$$= \frac{\binom{5}{5} \binom{64}{0}}{\binom{69}{5}} \cdot \frac{\binom{1}{0} \binom{25}{1}}{\binom{26}{1}} = \frac{1}{1168908.5}$$

$$= \left( \frac{1 \cdot 1}{11238513} \right) \left( \frac{1 \cdot 25}{26} \right)$$

THT 1  
#3

meta-code  
(process)  
how to  
solve  
prob. &  
stat. problems

- 1 identify all different sources of information
- 2 Choose T/F

Symbols carefully to stand for these information sources

- 1. who actually will be pardoned <sup>(truth)</sup> unknown
- what warden says data

A = (A gets pardon)  
B = (B \_\_\_\_\_)  
C = (C \_\_\_\_\_)

(W = X) =  
(warden says X)  
will not be pardoned

$$? = P(A | \underbrace{W=B}_{\text{data}}) \quad (\text{we want}) \quad (5)$$

↑ unknown

we know

data unknown

$$P(W=A | A) = 0$$

$$P(W=B | B) = 0$$

$$P(W=C | C) = 0$$

$$P(W=B | A) = \frac{1}{2}$$

$$P(W=C | A) = \frac{1}{2}$$

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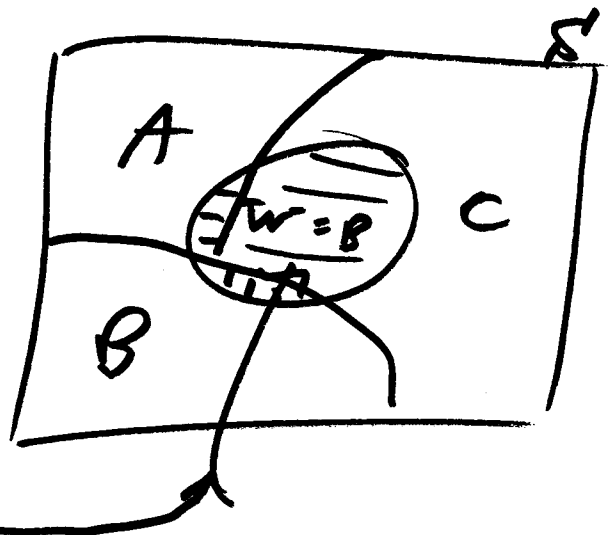
method III /  $P(A | W=B) = \frac{P(A) \cdot P(W=B|A)}{P(W=B)}$

$\swarrow \frac{1}{3}$        $\downarrow \frac{1}{2}$   
 $P(A)$        $P(W=B|A)$

~~the~~ warden's behavior ~~hard~~ to think about without knowing the truth

So: extend the conversation: partition <sup>the</sup> over truth (unknown) (6)

(we're computing  $P(W=B)$ )



$$P(W=B) = P(W=B \text{ and } A) + P(W=B \text{ and } B) + P(W=B \text{ and } C)$$

$P(\text{rain in se tomorrow} \mid \text{cold front moving in})$

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